$$\mathbf{s}(\mathbf{x},t) = \mathrm{Re}\sum_k (i\omega_k)^{-1}\mathbf{s}_k(\mathbf{x})\int_{-\infty}^{t} C_k(t')\exp\left[i\omega_k(t-t')\right]dt',$$